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Neural Networks and Fuzzy Logic

Assignment 1

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# Question 1.1. Discrete Perceptron training

Code behind Question 1.1. is located in the Appendix under Question 1.1. Discrete Perceptron training code.

## Calculate the final weight

The code in the Appendix provides the following output:

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 0.2309 | 0.3087 | 0.2150 | 0.3923 | 0.3892 | 0.3892 | 0.3892 | 0.4886 | 0.4886 | 0.4886 |
| 0.5839 | 0.6325 | 0.5857 | 0.7236 | 0.7128 | 0.7128 | 0.7128 | 0.7749 | 0.7749 | 0.7749 |
| 0.8436 | 0.8436 | 0.2345 | 0.2936 | 0.2812 | 0.2812 | 0.2812 | 0.2812 | 0.2812 | 0.2812 |
| 0.4764 | 0.4861 | 0.0644 | 0.1235 | 0.1204 | 0.1204 | 0.1204 | 0.1329 | 0.1329 | 0.1329 |
| -0.6475 | -0.5502 | -1.0188 | -0.8218 | -0.8372 | -0.8372 | -0.8372 | -0.7129 | -0.7129 | -0.7129 |

Note that by the 8th weight (which is essentially the 2nd pattern on its second time trip into the neural network) is providing a weight that does not change. This is seen on the 9th and 10th weight.

Hence the 10th weight is:

|  |
| --- |
| 10 |
| 0.4886 |
| 0.7749 |
| 0.2812 |
| 0.1329 |
| -0.7129 |

## Show that the final weight provides the correct classification of the entire training set

To determine if the final weight provides the correct classification for the training set above, the final weight was placed back into the network as the initial weight and the outputs were collected.

The ability to evolve was also commented out. See the Appendix for the code used.

The results are as follows:

|  |  |  |
| --- | --- | --- |
| Steps | Pattern | Error |
| 1 | 1 | 0 |
| 2 | 2 | 0 |
| 3 | 3 | 0 |
| 4 | 4 | -2 |
| 5 | 5 | 0 |
| 6 | 6 | 0 |

## Plot the pattern error curve

Calculating the pattern error curve is simply determining the error at which the system is evolving at.

This can be calculated via the equation of:

Where:

* Ep is the p-th error step, where p is the pattern
* dp is the expected output of the p-th pattern
* zp is the actual output from the activation function from the p-th pattern

In essence it is the variation of the actual output in comparison to the expected output.

As such some modification were made to the code to capture the pattern error run against an activation function and the expected output.

The following is the plotted pattern error. For the full set of plots and source code, please refer to the Appendix Question 1.1. discrete perceptron training code. See the patternErrors variable.

It is observed that the error fluctuates between the desired output and the actual output. Though it is also noted that as more cycles are progressively made, the less the errors become.

## Plot the cycle error curve

In accordance to the equation of:

Where:

* Ec is the error cycle
* P is the patterns that are processed
* dp is the expected output of the p-th pattern
* zp is the actual output from the p-th pattern
* Ep is the pattern cycle

In essence cycle error curve is assessing how for each “evolved” weight how well it fits the expected output of each input.

For the full specification please refer to the Appendix Question 1.1. Discrete perceptron training code and refer to the cycleErrors variable that stores the code.

Note that the 10 cycles in the code has been modified to 20 cycles observe a greater set of cycle errors per pattern that was passed through the neural network. Otherwise the cycles 1 and 2 represent the 10 cycle (see orange line).

The reduction of error to zero as shown in the 20 cycles is the result of overfitting the training data and reproducing the output exactly.

# Question 1.2. Continuous Perceptron training

The sigmoid activation function found in a discrete perception is replaced with a bipolar logistic function which is as follows:

An alternative representation of the function is:

## Calculate w7

The structure of the code was similar to the code listed in Question 1.1. except with a few changes to the core of the code to accept a continuous activation function (as noted above, a bipolar logistic function was used).

Below is the calculated weight at the 7th cycle of the program.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Cycle | Weight | | | | |
| 7 | 0.4421 | 0.6366 | 0.5754 | 0.3443 | -0.7502 |

For the full set of code and output generated, please refer to the Appendix for further details on the implementation under the heading of: Question 1.2.a and 1.2.b.

## Calculate the weight vector w301 after 50 cycles

Continuing the feedforward process for approximately 50 times, the weight evolution process is as follows:

| Cycles | Weight | | | | |
| --- | --- | --- | --- | --- | --- |
| 50 | 1.7325 | 1.0295 | -0.6459 | -0.1066 | -0.9328 |

For the full set of code and output generated, please refer to the Appendix for further details on the implementation under the heading of: Question 1.2.a and 1.2.b.

## Plot the cycle error curve

Given the equation of the error cycle:

The reference code can be found in the Appendix under the Question 1.2.a and 1.2.b code. The listed output can be found also in the Appendix under the Question 1.2.c cycle error.

Using Appendix Question 1.2.c cycle error data, the following is a plot of the errors across 54 cycles.

Note that the errors approach zero but never reach it due to the continuous activation function in contrast to that of the

## How would w7 and w301 classify the entire training set?

The weights have been modelled after the current set of data. As data is passed through the neural network, the weights would slowly converge on a function that approximates the generalised features of each given input.

Given the nature of a continuous activation function, that the resultant weights that are produced by the neural network converge on an extremely accurate result, the error is therefore minimised to a point that any further classification on the training data will result in overfitting.

Passing both weights back into the inputs to see their classification (see the appendix on the full code that was used to validate this claim), the classification is a lot different to that of a discrete perceptron and that mainly is derived from the fact that a continuous activation function is used, meaning that the outputs will always approach but never arrive at an exact result.

This means that the subsequent “classifications” will approach the desired values and this is shown in the data collected below from the code in the Appendix:

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Desired variation from output | 0 | 0 | 0 | 0 | 0 | 0 |
| w7 variation | 1.0219 | -1.2260 | 0.8174 | -1.1553 | 0.6504 | -0.8788 |
| w301 variation | 0.5548 | -0.3897 | 0.4915 | -0.8009 | 0.4538 | -0.5440 |

As noted that the variations are way off in the first 7 cycles (as the closer the variation is to 0, the more accurate it is). Though as shown below in the 301st cycle, the variation has decreased and is a lot closer to 0 than when it was initially.

# Question 2.1. Flight simulation

## Find R = M X A

The code that was used is as follows:

M = [0, 0.25, 0.75, 1, 0.75, 0.25, 0];

A = [0, 0.3, 0.6, 1, 0.6, 0.3, 0];

R = getRelation(M', A);

function output = getRelation(a, b)

output = min(a, b);

end

R is calculated to be via reading the minimum of both M’ and A:

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
|  | 0.725 | 0.73 | 0.735 | 0.74 | 0.745 | 0.75 | 0.755 |
| 8350 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8400 | 0 | 0.25 | 0.25 | 0.25 | 0.25 | 0.25 | 0 |
| 8450 | 0 | 0.3 | 0.6 | 0.75 | 0.6 | 0.3 | 0 |
| 8500 | 0 | 0.3 | 0.6 | 1 | 0.6 | 0.3 | 0 |
| 8550 | 0 | 0.3 | 0.6 | 0.75 | 0.6 | 0.3 | 0 |
| 8600 | 0 | 0.25 | 0.25 | 0.25 | 0.25 | 0.25 | 0 |
| 8650 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

## Find A1a = M1 ο R via max-min composition

Using the R matrix that was calculated from the previous question, it is reused to calculate A1a. For further details on the implementation of the fuzzy set please refer to Appendix Question 2.1.2 and 2.1.3 fuzzy generation code.

A1a is calculated to be:

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
|  | 0.725 | 0.73 | 0.735 | 0.74 | 0.745 | 0.75 | 0.755 |
| 8350 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8400 | 0 | 0.3000 | 0.5 | 0.5 | 0.5 | 0.3000 | 0.0000 |
| 8450 | 0 | 0.3000 | 0.6 | 0.8 | 0.6 | 0.3 | 0 |
| 8500 | 0 | 0.3000 | 0.6 | 1 | 0.6 | 0.3 | 0 |
| 8550 | 0 | 0.3000 | 0.6 | 0.6 | 0.6 | 0.3 | 0 |
| 8600 | 0 | 0.2000 | 0.2 | 0.2 | 0.2 | 0.2 | 0 |
| 8650 | 0 | 0.0000 | 0 | 0 | 0 | 0 | 0 |

Each row of M1’ (transposed) and R have their maximum values calculated and then combined via a minimum comparison between the two respective maximum values to form each cell of this matrix.

## Find A1b = M1 ο R via sum-product composition

Each column of a transposed M1 matrix is summed up and each column of the R matrix is summed up and then multiplied together to form A1b.

The code used to generate the fuzzy set below can be located in the Appendix under Question 2.1.2 and 2.1.3 fuzzy set generation code.

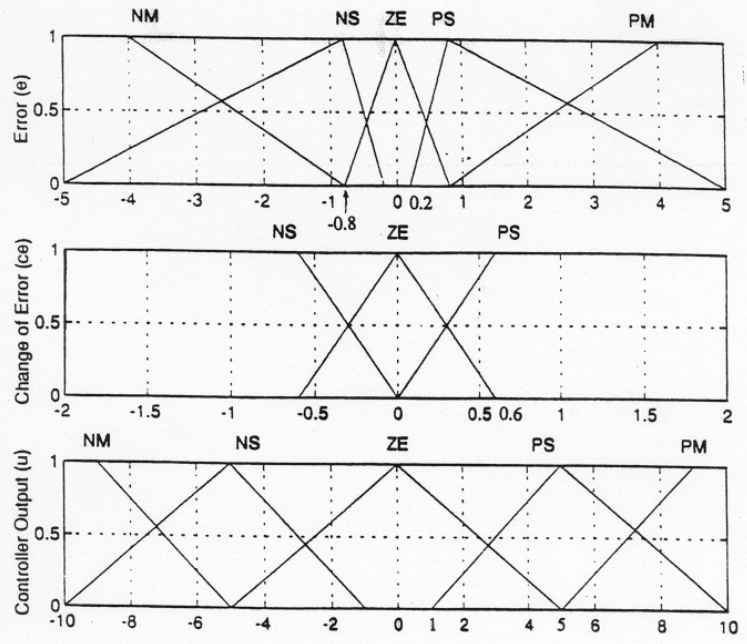
A1b is calculated to be:

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Altitude | 8350 | 8400 | 8450 | 8500 | 8550 | 8600 | 8650 |
| Mach | 0 | 4.34 | 7.13 | 9.3 | 7.13 | 4.34 | 0 |

# Question 2.2. Laser Beam Alignment

## Calculate the defuzzified voltage output via Mean of Maximum (MOM)

Given E = 3.2 and CE = -0.47 and given the inputs and output membership functions (with E and CE located on the diagrams as thick black lines).



### Fuzzification of E

Given that E is at 3.2 placing this on the graph. There are two lines that 3.2 intersects: PS and PM.

PS – (0.8, 1) to (5, 0) the equation therefore is:

E is calculated to be 3/7 or approximately 0.4286 on the PS membership function.

PM – (0.8, 0) to (4, 1) the equation therefore is:

E is calculated to be 0.75 when placing 3.2 into the PM equation.

Therefore, the fuzzified E at 3.2 is:

### Fuzzification of CE

Given that CE is at -0.47, there are two lines that intersect at that given value: NS and ZE.

NS – (-0.6, 1) to (0, 0) the equation therefore is:

CE is calculated to be approximately 0.7833 when placing -0.47 into the NS equation.

ZE – (-0.6, 0) to (0, 1) the equation therefore is:

CE is calculated to be approximately 0.2167 when placing -0.47 into the ZE equation.

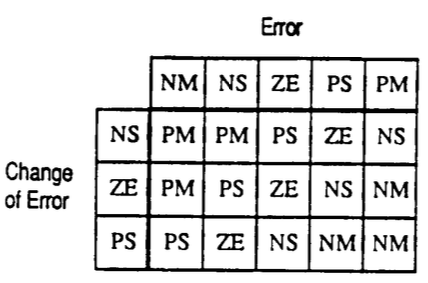
Therefore, the fuzzified CE at -0.47 is:

### Defuzzified output voltage via Mean of Maximum

Tabulating the above results we get:

|  |  |  |  |
| --- | --- | --- | --- |
| Rules | E | CE | U(MOM) |
| 1 | 0.4286/PS | 0.7833/NS | 0.3357/ZE |
| 2 | 0.4286/PS | 0.2167/ZE | 0.0929/NS |
| 3 | 0.75/PM | 0.7833/NS | 0.5875/NS |
| 4 | 0.75/PM | 0.2167/ZE | 0.1625/NM |

Multiplying each value of E with CE produces a U value for the U(MOM) column. The associative memories is determined via the given associative memories identity.



Using the Controller output membership function to quantify the values of ZE (0), NS (-5) and NM (9), the following is the output voltage.

Therefore, the output voltage, V is calculated to be approximately -1.6456.

## Calculate the defuzzified voltage output via Centre of Area (COA)

Given e = 3.2 and ce = -0.47

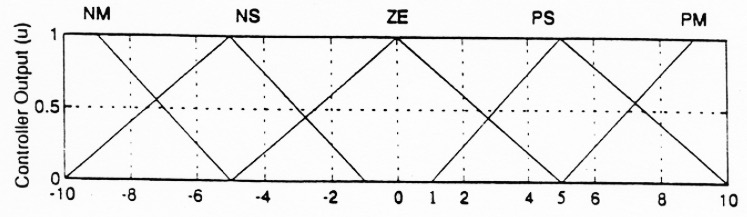
### Fuzzification of E and CE

Borrowing from the previous calculations of E and CE, the fuzzified values of E and CE respectively are:

### Total Area

Tabulating the fuzzified values and taking the minimum of each value:

|  |  |  |  |
| --- | --- | --- | --- |
| Rules | E | CE | U(COA) |
| 1 | 0.4286/PS | 0.7833/NS | 0.4286/ZE |
| 2 | 0.4286/PS | 0.2167/ZE | 0.2167/NS |
| 3 | 0.75/PM | 0.7833/NS | 0.75/NS |
| 4 | 0.75/PM | 0.2167/ZE | 0.2167/NM |



For completion’s sake the equations of the three slopes highlighted by the coloured area are:

1. Positive NS slope up:
2. Negative NS slope down:
3. Negative ZE slope down:

These formulas have been formed based on the points of each of the slopes located on the Controller output membership function.

Coordinates as listed from left to right are:

1. -10, 0
2. -10, 0.2167 (gained from rule 4)
3. -8.9165, 0.2167 (replacing 0.2167 into positive NS slope up equation)
4. -6.25, 0.75 (replacing 0.75 into positive NS slope up equation)
5. -4, 0.75 (replacing 0.75 into negative NS slope down equation)
6. -2.7144, 0.4286 (replacing 0.4286 into negative NS slope down equation)
7. 2.857, 0.4286 (replacing 0.4286 into negative ZE slope down equation)
8. 5, 0

Going from left to right the elements of COA (Center of Area) are:

1

3

5

2

4

6

Area1 = 0.2167 \* 3.75 = 0.8126

3.75 comes from 10 – 6.25

Area2 = (0.75 – 0.2167) \* (8.9165 – 6.25) / 2 = 0.711

Area3 = 0.75 \* 2.25 = 1.6875

2.25 comes from 6.25 – 4

Area4 = (4 – 2.7144) \* (0.75 – 0.4286) / 2 = 0.2066

Area 5 = (2.7144 + 2.857) \* 0.4286 = 2.3879

2.7144 + 2.857 comes from the crossing of the origin, meaning the distance is the distance between the two points.

Area 6 = (5 – 2.857) \* 0.4286 / 2 = 0.9185

Total area = 0.8126 + 0.711 + 1.6875 + 0.2066 + 2.3879 + 0.9185 = 6.5086

Therefore, the total area is 6.5086.

### Total Moment

Generalising the total area into a formula you get:

So to find the Total moment, you integrate the Total area to get the Total moment.

Hence the Total moment is depicted as:

Substituting all the values will give you:

Total moment = (0.2348) + (4.6875-1.9322) + (1.6875) + (-1.1634+3) + (2.3879) + (0-1.2245)

Total moment = 7.6908

### Defuzzified output voltage

This is the Total moment over the Total area.

Total moment = 7.6908

Total area = 6.5086

Defuzzified output voltage = 7.6908 / 6.5086 = 1.1816

# Appendix

## Question 1.1. Discrete Perceptron Training code

clc;

clear;

% augmented input vectors

x1 = [0.8, 0.5, 0, 0.1, 1];

x2 = [0.2, 0.1, 1.3, 0.9, 1];

x3 = [0.9, 0.7, 0.3, 0.3, 1];

x4 = [0.2, 0.7, 0.8, 0.2, 1];

x5 = [1, 0.8, 0.5, 0.7, 1];

x6 = [0, 0.2, 0.3, 0.6, 1];

% each of the augmented vectors are placed into a single vector to churn

% through

y = [x1; x2; x3; x4; x5; x6]';

% associated outputs

d = [1, -1, 1, -1, 1, -1];

% given lambda

lambda = 1.5;

% given cycles

cycles = 10;

% starting weight

w = [0.2309, 0.5839, 0.8436, 0.4764, -0.6475]';

% a counter for the cycles to be measure against

inputCounter = 1;

% setting up the output matrix

[dRows, dCols] = size(x1');

output = zeros(dRows, cycles);

cycleErrors = zeros(1, (cycles - mod(cycles, 6))/6 + 1);

cycleErrorIndex = 1;

patternErrors = zeros(cycles, 3);

for index = 1:cycles

output(:, index) = w;

[w, cycleError] = variablecorrection(w, lambda, y(:, inputCounter), d(:, inputCounter));

cycleErrors(:, cycleErrorIndex) = cycleErrors(:, cycleErrorIndex) + 0.5 \* (cycleError)^2;

patternErrors(index, :) = [index, inputCounter, cycleError];

inputCounter = inputCounter + 1;

if inputCounter > 6

inputCounter = 1;

cycleErrorIndex = cycleErrorIndex + 1;

end

end

disp(output);

disp(cycleErrors);

% weight correction formula given

function [output, error] = variablecorrection(w, lambda, y, d)

error = (d - sign(w' \* y));

output = w + 0.5 \* (lambda \* abs(w' \* y) / (y' \* y)) \* error \* y;

end

## Question 1.1.b pattern validation code

clc;

clear;

% augmented input vectors

x1 = [0.8, 0.5, 0, 0.1, 1];

x2 = [0.2, 0.1, 1.3, 0.9, 1];

x3 = [0.9, 0.7, 0.3, 0.3, 1];

x4 = [0.2, 0.7, 0.8, 0.2, 1];

x5 = [1, 0.8, 0.5, 0.7, 1];

x6 = [0, 0.2, 0.3, 0.6, 1];

% each of the augmented vectors are placed into a single vector to churn

% through

y = [x1; x2; x3; x4; x5; x6]';

% associated outputs

d = [1, -1, 1, -1, 1, -1];

% given lambda

lambda = 1.5;

% given cycles

cycles = 6;

% starting weight

%w = [0.2309, 0.5839, 0.8436, 0.4764, -0.6475]';

w = [0.488600000000000;0.774900000000000;0.281200000000000;0.132900000000000;-0.712900000000000];

% a counter for the cycles to be measure against

inputCounter = 1;

% setting up the output matrix

[dRows, dCols] = size(x1');

output = zeros(dRows, cycles);

cycleErrors = zeros(1, (cycles - mod(cycles, 6))/6 + 1);

cycleErrorIndex = 1;

patternErrors = zeros(cycles, 3);

for index = 1:cycles

output(:, index) = w;

[w, cycleError] = variablecorrection(w, lambda, y(:, inputCounter), d(:, inputCounter));

cycleErrors(:, cycleErrorIndex) = cycleErrors(:, cycleErrorIndex) + 0.5 \* (cycleError)^2;

patternErrors(index, :) = [index, inputCounter, cycleError];

disp([index, d(:, inputCounter), cycleError]);

disp(y(:, inputCounter));

inputCounter = inputCounter + 1;

if inputCounter > 6

inputCounter = 1;

cycleErrorIndex = cycleErrorIndex + 1;

end

end

disp(output);

disp(cycleErrors);

% weight correction formula given

function [output, error] = variablecorrection(w, lambda, y, d)

error = (d - sign(w' \* y));

%output = w + 0.5 \* (lambda \* abs(w' \* y) / (y' \* y)) \* error \* y;

output = w;

end

## Question 1.1.c pattern errors

This is the pattern errors generated from each of the patterns.

|  |  |  |
| --- | --- | --- |
| Steps | Pattern Number | Error generated |
| 1 | 1 | 2 |
| 2 | 2 | -2 |
| 3 | 3 | 2 |
| 4 | 4 | -2 |
| 5 | 5 | 0 |
| 6 | 6 | 0 |
| 7 | 1 | 2 |
| 8 | 2 | 0 |
| 9 | 3 | 0 |
| 10 | 4 | -2 |

## Question 1.2.a and 1.2.b continuous perceptron weight generation code

% see tut1 for assistance

clc;

clear;

% augmented input vectors

x1 = [0.8, 0.5, 0, 0.1, 1];

x2 = [0.2, 0.1, 1.3, 0.9, 1];

x3 = [0.9, 0.7, 0.3, 0.3, 1];

x4 = [0.2, 0.7, 0.8, 0.2, 1];

x5 = [1, 0.8, 0.5, 0.7, 1];

x6 = [0, 0.2, 0.3, 0.6, 1];

% each of the augmented vectors are placed into a single vector to churn

% through

y = [x1; x2; x3; x4; x5; x6]';

% associated outputs

d = [1, -1, 1, -1, 1, -1];

% given learning constant

learningConstant = 0.25;

% given cycles

cycles = 50;

% starting weight

w = [0.2309, 0.5839, 0.8436, 0.4764, -0.6475]';

% a counter for the cycles to be measure against

inputCounter = 1;

% setting up the output matrix

[dRows, dCols] = size(x1');

output = zeros(dRows, cycles);

% note that there are six patterns

cycleErrors = zeros(1, cycles/6);

cycleIndex = 1;

for index = 1:cycles

output(:, index) = w;

[w, cycleError] = continuousCorrection(w, learningConstant, y(:, inputCounter), d(:, inputCounter));

cycleErrors(:, cycleIndex) = cycleErrors(:, cycleIndex) + cycleError^2;

inputCounter = inputCounter + 1;

if inputCounter > size(d)

%disp([inputCounter, index, inputCounter > size(d), cycleIndex]);

inputCounter = 1;

cycleErrors(:, cycleIndex) = 0.5 \* cycleErrors(:, cycleIndex);

cycleIndex = cycleIndex + 1;

end

end

disp(output);

disp(cycleErrors);

% weight correction formula given, need to look at activation functions

function [outputWeight, error] = continuousCorrection(weight, learningConstant, input, expectedValue)

v = weight' \* input;

z = (2 / (1 + exp(-v))) - 1;

error = expectedValue - z;

rate = 0.5\*(1 - z^2);

r = error \* rate;

outputWeight = weight + learningConstant \* r \* input;

end

## Question 1.2.a and 1.2.b weight generation

This is every weight that has been cycled through via the code referenced on the previous page.

| Cycle | Weight | | | | |
| --- | --- | --- | --- | --- | --- |
| 1 | 0.2309 | 0.5839 | 0.8436 | 0.4764 | -0.6475 |
| 2 | 0.3367 | 0.6500 | 0.8436 | 0.4896 | -0.5153 |
| 3 | 0.3089 | 0.6361 | 0.6635 | 0.3649 | -0.6539 |
| 4 | 0.3972 | 0.7048 | 0.6929 | 0.3943 | -0.5558 |
| 5 | 0.3676 | 0.6012 | 0.5745 | 0.3647 | -0.7038 |
| 6 | 0.4421 | 0.6608 | 0.6117 | 0.4169 | -0.6293 |
| 7 | 0.4421 | 0.6366 | 0.5754 | 0.3443 | -0.7502 |
| 8 | 0.5443 | 0.7004 | 0.5754 | 0.3571 | -0.6225 |
| 9 | 0.5147 | 0.6856 | 0.3831 | 0.2240 | -0.7705 |
| 10 | 0.6046 | 0.7556 | 0.4131 | 0.2539 | -0.6706 |
| 11 | 0.5761 | 0.6557 | 0.2990 | 0.2254 | -0.8132 |
| 12 | 0.6575 | 0.7209 | 0.3398 | 0.2825 | -0.7317 |
| 13 | 0.6575 | 0.7003 | 0.3089 | 0.2208 | -0.8345 |
| 14 | 0.7542 | 0.7608 | 0.3089 | 0.2329 | -0.7137 |
| 15 | 0.7278 | 0.7476 | 0.1370 | 0.1138 | -0.8459 |
| 16 | 0.8140 | 0.8146 | 0.1657 | 0.1426 | -0.7501 |
| 17 | 0.7874 | 0.7213 | 0.0591 | 0.1159 | -0.8834 |
| 18 | 0.8691 | 0.7867 | 0.0999 | 0.1731 | -0.8017 |
| 19 | 0.8691 | 0.7691 | 0.0736 | 0.1204 | -0.8896 |
| 20 | 0.9581 | 0.8247 | 0.0736 | 0.1315 | -0.7783 |
| 21 | 0.9371 | 0.8143 | -0.0626 | 0.0372 | -0.8831 |
| 22 | 1.0154 | 0.8752 | -0.0365 | 0.0633 | -0.7961 |
| 23 | 0.9904 | 0.7875 | -0.1367 | 0.0382 | -0.9213 |
| 24 | 1.0671 | 0.8489 | -0.0983 | 0.0920 | -0.8446 |
| 25 | 1.0671 | 0.8334 | -0.1215 | 0.0455 | -0.9219 |
| 26 | 1.1471 | 0.8834 | -0.1215 | 0.0555 | -0.8219 |
| 27 | 1.1311 | 0.8754 | -0.2257 | -0.0166 | -0.9021 |
| 28 | 1.2002 | 0.9292 | -0.2027 | 0.0065 | -0.8252 |
| 29 | 1.1765 | 0.8461 | -0.2977 | -0.0173 | -0.9440 |
| 30 | 1.2465 | 0.9021 | -0.2627 | 0.0317 | -0.8740 |
| 31 | 1.2465 | 0.8882 | -0.2836 | -0.0101 | -0.9436 |
| 32 | 1.3177 | 0.9327 | -0.2836 | -0.0012 | -0.8546 |
| 33 | 1.3054 | 0.9265 | -0.3637 | -0.0566 | -0.9163 |
| 34 | 1.3663 | 0.9739 | -0.3433 | -0.0363 | -0.8486 |
| 35 | 1.3436 | 0.8946 | -0.4339 | -0.0590 | -0.9618 |
| 36 | 1.4072 | 0.9455 | -0.4021 | -0.0145 | -0.8982 |
| 37 | 1.4072 | 0.9328 | -0.4212 | -0.0526 | -0.9618 |
| 38 | 1.4705 | 0.9723 | -0.4212 | -0.0447 | -0.8827 |
| 39 | 1.4609 | 0.9675 | -0.4836 | -0.0879 | -0.9307 |
| 40 | 1.5150 | 1.0096 | -0.4656 | -0.0699 | -0.8706 |
| 41 | 1.4934 | 0.9340 | -0.5520 | -0.0915 | -0.9786 |
| 42 | 1.5513 | 0.9804 | -0.5230 | -0.0510 | -0.9206 |
| 43 | 1.5513 | 0.9686 | -0.5406 | -0.0861 | -0.9792 |
| 44 | 1.6080 | 1.0041 | -0.5406 | -0.0790 | -0.9084 |
| 45 | 1.6004 | 1.0002 | -0.5900 | -0.1133 | -0.9464 |
| 46 | 1.6489 | 1.0380 | -0.5738 | -0.0971 | -0.8925 |
| 47 | 1.6283 | 0.9660 | -0.6562 | -0.1177 | -0.9954 |
| 48 | 1.6815 | 1.0085 | -0.6296 | -0.0804 | -0.9422 |
| 49 | 1.6815 | 0.9976 | -0.6459 | -0.1130 | -0.9965 |
| 50 | 1.7325 | 1.0295 | -0.6459 | -0.1066 | -0.9328 |

## Question 1.2.c cycle error production

This is the error generated at each cycle of the evolution of the neural network.

| Cycle | Cumulative Patterns | Error |
| --- | --- | --- |
| 1 | 6 | 3.6064 |
| 2 | 12 | 3.0135 |
| 3 | 18 | 2.4616 |
| 4 | 24 | 2.0177 |
| 5 | 30 | 1.6858 |
| 6 | 36 | 1.4391 |
| 7 | 42 | 1.2520 |
| 8 | 48 | 1.1065 |
| 9 | 50 | 0.5175 (0.9904) |

Note that there the patterns are 6, so every 6 patterns, the cycle error would be captured, hence the full 9th cycle (requiring the 54th pattern to cycle through) is 0.5175 since there isn’t enough data to capture together yet. Hence it is considered an incomplete cycle as noted by the number of patterns it has cycled through.

Though, the second number in the brackets is what would have happened if you cycled through 54 cycles instead of the listed 50.

## Question 1.2.d validating the training set code

clc;

clear;

seventhWeight = [0.442131840727600;0.636597872834342;0.575441294301345;0.344346399188018;-0.750222787022720];

finalWeight = [1.73253526080533;1.02953015227645;-0.645882485236181;-0.106634592428199;-0.932766308404683];

% augmented input vectors

x1 = [0.8, 0.5, 0, 0.1, 1];

x2 = [0.2, 0.1, 1.3, 0.9, 1];

x3 = [0.9, 0.7, 0.3, 0.3, 1];

x4 = [0.2, 0.7, 0.8, 0.2, 1];

x5 = [1, 0.8, 0.5, 0.7, 1];

x6 = [0, 0.2, 0.3, 0.6, 1];

% each of the augmented vectors are placed into a single vector to churn

% through

y = [x1; x2; x3; x4; x5; x6]';

% associated outputs

d = [1, -1, 1, -1, 1, -1];

[yRows, yCols] = size(y);

seventhWeightErrors = zeros(1, yCols);

finalWeightErrors = zeros(1, yCols);

for index = 1:yCols

finalWeightErrors(:, index) = validation(finalWeight, y(:,index), d(:, index));

seventhWeightErrors(:, index) = validation(seventhWeight, y(:,index), d(:, index));

end

disp(finalWeightErrors);

disp(seventhWeightErrors);

function error = validation(weight, input, expectedValue)

v = weight' \* input;

z = (2 / (1 + exp(-v))) - 1;

disp([expectedValue, z]);

error = expectedValue - z;

end

## Question 2.1.2 and 2.1.3 fuzzy set generation code

clc;

clear;

M1 = [0, 0.5, 0.8, 1, 0.6, 0.2, 0];

R = [0,0,0,0,0,0,0;0,0.250000000000000,0.250000000000000,0.250000000000000,0.250000000000000,0.250000000000000,0;0,0.300000000000000,0.600000000000000,0.750000000000000,0.600000000000000,0.300000000000000,0;0,0.300000000000000,0.600000000000000,1,0.600000000000000,0.300000000000000,0;0,0.300000000000000,0.600000000000000,0.750000000000000,0.600000000000000,0.300000000000000,0;0,0.250000000000000,0.250000000000000,0.250000000000000,0.250000000000000,0.250000000000000,0;0,0,0,0,0,0,0];

% 2.1.2 Find A1a = M1 o R using max-min - apply max first then min overall

A1a = maxMinComposition(M1', R);

% 2.1.3 Find A1b = M1 o R using sum-product - sum each row, then multiply

A1b = sumProductComposition(M1', R);

disp(A1a);

disp(A1b);

function output = maxMinComposition(a, b)

output = min(max(a,[],2),... % read the rows of a

max(b,[],1)); % read the columns of b

end

function output = sumProductComposition(a, b)

output = sum(a) \* sum(b);

end